

University of Information Technology & Sciences (UITS)

Faculty of Science and Engineering

Department of Computer Science and Engineering

Program: B.Sc. in CSE

Term Final Examination, Spring - 2025

Course Title: Discrete Mathematics

Course Code: CSE 0541123

Marks: 50

Time: 3(three) hours

(Answer all questions)

1. a) Let $Q(x)$ be the statement " $3x + 1 > 2x$." If the domain consists of all integers, find the truth values of the following statements and explain with an example. [05]

a) $Q(-1)$ b) $\exists x Q(x)$ c) $\forall x Q(x)$

d) $\exists x \neg Q(x)$ e) $\forall x \neg Q(x)$

b) Translate these statements into English, where $R(x)$ is "x is a leopard" and $H(x)$ is "x jumps" and the domain consists of all animals. [05]

a) $\forall x (R(x) \rightarrow H(x))$ b) $\forall x (R(x) \wedge H(x))$

c) $\exists x (R(x) \rightarrow H(x))$ d) $\exists x (R(x) \wedge H(x))$

e) $\exists x (H(x) \rightarrow R(x))$

$$L(x) = R(x)$$

$$J(x) = H(x)$$

2. a) Prove that if n is a composite integer then it has a divisor not great than \sqrt{n} . [05]

b) For the sum $1 + 3 + 5 + \dots + (2n - 1)$, formulate a hypothesis and prove it by induction. [05]

3. a) Let $A = \{1, 2, 4, 5, 6, 7, 8\}$ and $B = \{1, 2, 3, 7, 9\}$. Find - [05]

a) $A \cup B$. b) $A \cap B$. c) $A - B$. d) $B - A$. e) $(A - B) \cup (B - A)$

b) Define function. Explain with example each of the following functions from \mathbb{N} to \mathbb{N} that is - [05]

a) one-to-one but not onto.

b) onto but not one-to-one.

c) both onto and one-to-one.

d) neither one-to-one nor onto.

4. a) Contradict the hypothesis that there are exactly k primes. [05]

b) Prove that any integer $n \geq 1$ can be represented using 0's and 1's in decimal number system. [05]

5. a) Consider the following congruences - [05]
 $x \equiv 3 \pmod{5}$ $x \equiv 1 \pmod{7}$ $x \equiv 1 \pmod{3}$

Calculate the value of x using Chinese Remainder Theorem.

b) Using shift cipher with $k=5$ that is $f(p) = (p+5) \pmod{26}$ produce the secret message for "SEE YOU AFTER THE CLASS IN THE PARK". [05]