

University of Information Technology & Sciences
Faculty of Science and Engineering
Department of CSE
Midterm Examination, Spring- 2024
Course Title: Ordinary and Partial Differential Equations
Course Code: MAT 165

Marks: 20

Time: 1(One)hour

Answer all questions.

1. (a) Define order and degree of a differential equation. State the order and degree of the following equations and whether the equation is linear or nonlinear: [4]

(i) $\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^3 = 0$ (ii) $\left(\frac{dr}{ds}\right)^3 = \sqrt{\frac{d^2r}{ds^2} + 1}$.

- (b) Form the differential equations of the following equation: $y = c(x - c)^2$, where c is arbitrary constant. [3]

- (c) Identify the exactness and Solve the differential equation; [3]

$$(x^2 - 2xy + 3y^2)dx + (4y^3 + 6xy - x^2)dy = 0.$$

2. (a) Solve the differential equations: [10]

i) $\frac{dy}{dx} + 3x^2y = 4x^2y^2$.

ii) $(x^3 + 3xy^2)dx + (y^3 + 3x^2y)dy = 0$